

Analysis of Imperceptibility and Robustness of DFT-PSO Based QR Code Watermarking on Digital Signature Images

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Abstract

Electronic document forgery, including manipulation of digital signatures, has been reported as a measurable component of cybercrime cases in Indonesia. This study analyzes the imperceptibility and robustness characteristics of a watermarking scheme that embeds a QR Code containing identity information into a digital signature image using the Discrete Fourier Transform (DFT), restricted to the mid-frequency region of the spectrum. The embedding strength parameter (α) was determined using Particle Swarm Optimization (PSO), with a fitness function combining Peak Signal-to-Noise Ratio (PSNR) and Normalized Cross-Correlation (NCC) across simulated attack conditions. A manually configured baseline ($\alpha = 0.05$) produced a PSNR of 39.25 dB and an NCC of 1.0000 under no-attack conditions. After PSO optimization, the selected α (0.1007) produced a PSNR of 51.15 dB and an NCC of 0.9499 under no-attack conditions, corresponding to an 11.90 dB increase in PSNR relative to the baseline. Under six simulated attack conditions, JPEG compression at quality factors 75 and 50, Gaussian noise at standard deviations 10 and 25, rotation at 5°, and brightness adjustment of +50 NCC values ranged from 0.0006 to 0.3690. A comparative experiment using an academic certificate image as the cover image yielded an NCC of 0.7500 under JPEG compression at a quality factor of 75, indicating that the cover image's texture complexity influences watermark robustness. These findings indicate that PSO-based optimization of the DFT embedding parameter yields a measurable improvement in imperceptibility, while robustness to attacks remains constrained by the non-blind extraction method employed.

Keywords: digital image watermarking, DFT, PSO, QR code, imperceptibility, robustness analysis.

I. INTRODUCTION

Documents in digital form are increasingly used in administrative and legal contexts, including those bearing handwritten signatures. In Indonesia, electronic document forgery accounts for approximately 22% of digital crime reports recorded by the National Cyber and Crypto Agency in 2023 [1]. One documented case occurred at the Jakarta Administrative Court in 2022, where forged government documents were identified through forensic metadata and digital signature analysis [1]. Separately, classifier-based methods for detecting forged handwritten signatures report persistent difficulty in distinguishing forged from genuine samples, due to natural variation among genuine signatures from the same individual [2]. These findings indicate a measurable gap in signature-level authentication mechanisms for digital documents.

Digital image watermarking embeds auxiliary information into an image for the purpose of authentication or ownership verification. Watermarking schemes are classified as blind, where the watermark is extracted without reference to the original image, or non-blind, which requires the original image during extraction

[3]. In the additive embedding method, the watermark is added to image components via a mathematical operation, with a scaling factor controlling embedding strength [3].

Among frequency-domain methods, watermark embedding in the Discrete Fourier Transform (DFT) domain has been reported to provide resistance to rotation, scaling, and translation [4]. Embedding restricted to the mid-frequency region has been used to avoid the high sensitivity of low-frequency coefficients to modification and the susceptibility of high-frequency coefficients to attenuation under compression [4]. Selection of the embedding strength parameter, denoted α , is commonly performed manually; this approach requires repeated trial-and-error and does not generalize across different cover images [5].

Manuel et al. applied Particle Swarm Optimization (PSO) to determine α in a DFT-based watermarking scheme, reporting changes in PSNR and NCC values relative to manually configured baselines [5]. Wang et al. applied PSO with a fitness function combining PSNR and NCC across multiple simulated attacks in a medical

image watermarking scheme using a wavelet-based transform [6], indicating that PSO-based parameter search has been applied across more than one transform domain.

Robustness against image-processing operations is commonly assessed by simulating attacks such as JPEG compression, noise addition, and geometric distortion, then measuring the similarity between the original and extracted watermark. Strength-balanced optimization approaches have been proposed to address the trade-off between imperceptibility and robustness under such conditions, demonstrating that watermark strength can be adaptively adjusted according to the specific distortion intensity a watermarked image is expected to undergo, rather than fixed at a single predetermined value [7]. This indicates that the relationship between embedding strength and robustness is not fixed, but can be optimized according to the specific distortion conditions involved.

The choice of frequency band for embedding has also been reported to affect robustness outcomes differently depending on the type of distortion applied. Mid-frequency embedding has been associated with a balance between visual quality and resistance to common distortions, since low-frequency coefficients carry most of the image energy and are highly sensitive to modification, whereas high-frequency coefficients are more susceptible to attenuation under compression [4]. This pattern is consistent with the rationale for restricting the optimized embedding strength α to the mid-frequency region in the present study, in contrast to schemes that embed across the entire frequency spectrum without optimization-guided coefficient selection [5].

QR Code has been used as an information carrier in document authentication schemes. Yulianto and Wendanto reported a QR Code-based digital signature scheme using cryptographic hashing and encryption, with extraction tested under rotation, sharpening, and Gaussian noise conditions [8]. Sanivarapu et al. embedded a QR Code containing a cryptographic key pair into a host image for ownership verification [9]. Both schemes rely on cryptographic embedding rather than frequency-domain watermarking.

Three gaps follow from this review. First, DFT-based watermarking with manually configured α has been reported without an automated optimization procedure in [3] and partially addressed in [5]. Second, PSO-based parameter optimization has been reported for wavelet-based transforms [6], with limited reporting for mid-frequency DFT embedding specifically. Third, QR Code-based authentication schemes reported in [9] and [7] use cryptographic embedding rather than imperceptible watermarking. This study analyzes the imperceptibility and robustness characteristics of a QR

Code watermarking scheme applied to digital signature images. The scheme embeds a QR Code payload into the mid-frequency region of the DFT domain, with the embedding strength parameter α determined through PSO optimization. PSNR is used to quantify imperceptibility, and NCC is used to measure watermark recoverability under six simulated attack conditions. An additional comparative experiment is conducted using an academic certificate image to examine whether cover image texture complexity influences robustness outcomes.

II. METHOD

A. Dataset

The dataset consisted of one grayscale digital signature image used as the cover image and one QR Code image containing an encoded identity string used as the watermark payload. Both images were represented in 8-bit grayscale format. Figure 1. shows the system pipeline.

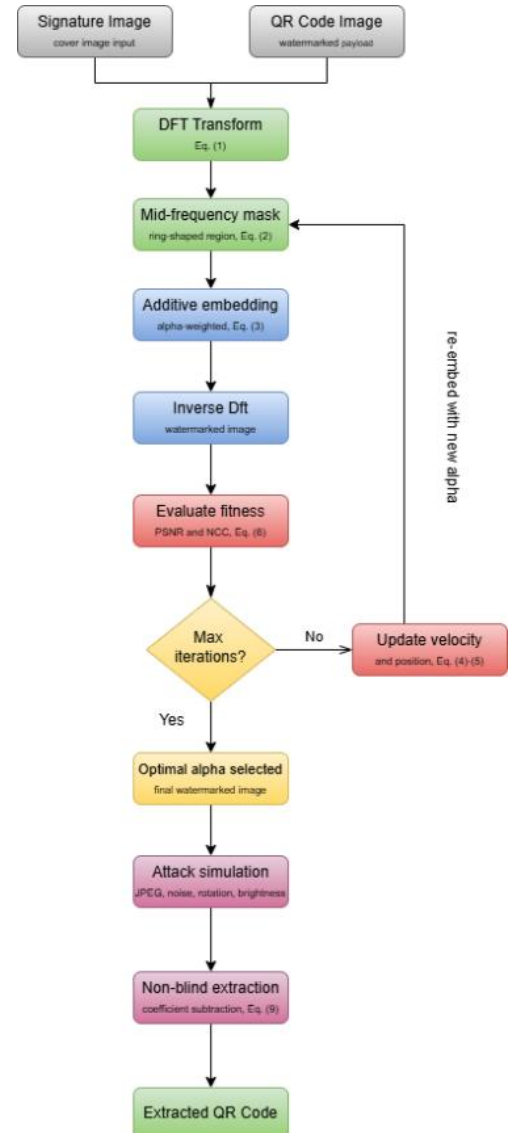


Figure 1. System flowchart DFT-PSO Watermarking Scheme

B. DFT-Based Mid-Frequency Embedding

The cover image was converted to the frequency domain using the two-dimensional DFT:

$$F(u, v) = \sum_{x=0}^{M-1} \sum_{y=0}^{N-1} f(x, y) e^{-j2\pi\left(\frac{ux}{M} + \frac{vy}{N}\right)} \quad (1)$$

where $f(x, y)$ is the spatial-domain pixel value, $F(u, v)$ is the frequency-domain coefficient, and M, N are the image dimensions. The spectrum was shifted to center the zero-frequency component, producing $F_{shift}(u, v)$.

Embedding was restricted to a ring-shaped region defined as:

$$Mask(u, v) = \begin{cases} 1, & r_{min}R \leq d(u, v) \leq r_{max}R \\ 0, & \text{otherwise} \end{cases} \quad (2)$$

where $d(u, v)$ is the distance from coefficient (u, v) to the spectrum center, $R = \min(M, N)/2$, $r_{min} = 0.10$, and $r_{max} = 0.40$. This range was selected based on the reported sensitivity of low-frequency coefficients to modification and the reported attenuation of high-frequency coefficients under compression [4].

The QR Code, resized to 64×64 pixels, was embedded using:

$$F_w(u, v) = F_{shift}(u, v) + \alpha \cdot Q(u, v), \quad \forall (u, v) \in Mask \quad (3)$$

where $Q(u, v)$ is the resized QR Code pixel value and α is the embedding strength factor [3]. The watermarked image was obtained via inverse shift and inverse DFT.

C. Parameter Optimization Using PSO

The value of α was determined using PSO rather than manual configuration [5]. Each particle i represents a candidate α value, updated according to:

$$v_i^{t+1} = wv_i^t + c_1r_1(p_i - x_i^t) + c_2r_2(g - x_i^t) \quad (4)$$

$$x_i^{t+1} = x_i^t + v_i^{t+1} \quad (5)$$

where w is the inertia weight, c_1 and c_2 are acceleration coefficients, r_1 and r_2 are random values in $[0, 1]$, p_i is the personal best position, and g is the global best position [10]. The swarm consisted of 15 particles over 25 iterations, with $\alpha \in [0.05, 0.50]$.

Fitness was calculated as:

$$Fitness(\alpha) = w_1 \cdot \frac{PSNR(\alpha)}{PSNR_{max}} + w_2 \cdot NCC(\alpha) \quad (6)$$

with $w_1 = 0.25$, $w_2 = 0.75$, and $NCC(\alpha)$ averaged across four simulated attack conditions during optimization. Candidates producing PSNR below 30 dB

were assigned a fitness value of zero. Fitness evaluation (6) and parameter update (4) (5) were repeated for 25 iterations, after which the global best α was recorded.

D. Evaluation Metrics

PSNR was calculated as:

$$PSNR = 10 \log_{10} \left(\frac{255^2}{MSE} \right),$$

$$MSE = \frac{1}{MN} \sum_x \sum_y [f(x, y) - f_w(x, y)]^2 \quad (7)$$

NCC was calculated as:

$$NCC = \frac{\sum_x \sum_y W(x, y) W'(x, y)}{\sqrt{\sum_x \sum_y W(x, y)^2 \cdot \sum_x \sum_y W'(x, y)^2}} \quad (8)$$

where $W(x, y)$ and $W'(x, y)$ are the original and extracted watermark pixel values [11].

E. Extraction and Robustness Testing

Extraction subtracted the cover image's DFT coefficients from the (possibly attacked) watermarked image's coefficients within the mask region, followed by inverse DFT:

$$Q'(u, v) = \frac{F'_w(u, v) - F_{shift}(u, v)}{\alpha}, \quad \forall (u, v) \in Mask \quad (9)$$

The result was normalized and binarized using Otsu's method before NCC computation. Six attack conditions were tested: JPEG compression at quality factors 75 and 50, Gaussian noise at standard deviations 10 and 25, rotation at 5° , and brightness adjustment of ± 0.50 [3]. NCC values were categorized as >0.85 , >0.70 , >0.50 , and ≤ 0.50 following thresholds reported in prior watermarking evaluation studies [11].

III. RESULT

A. Baseline DFT Implementation

With manually configured $\alpha = 0.05$ and full spectrum embedding, the watermarked image produced a PSNR of 39.25 dB. Under no-attack conditions, extraction produced an NCC of 1.0000, as summarized in Table 1.

Table 1. Baseline DFT Performance vs Target

Metric	Target	Value
PSNR	> 35 dB	39.25 dB
NCC	> 0.85	1.000



Figure 2. Visualization DFT Baseline

B. PSO Optimized Mid-Frequency Embedding

Applying mid-frequency embedding with PSO-based optimization, the algorithm converged at iteration 15 of 25, with a recorded global best $\alpha = 0.1007$. Under this configuration, PSNR was 51.15 dB and NCC was 0.9499 under no-attack conditions. This corresponds to a PSNR increase of 11.90 dB relative to the manually configured baseline.

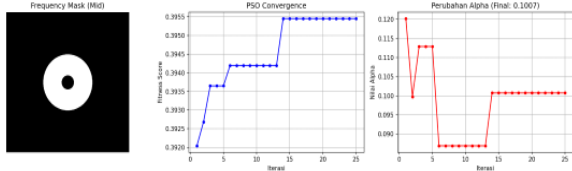


Figure 3. PSO Convergence + Alpha

C. Robustness Testing

Table 2 reports NCC values for six attack conditions using $\alpha = 0.1007$.

Table 2. NCC Under Six Attack Conditions

Attack	NCC	Status
JPEG (Q=75)	0.3690	Weak
JPEG (Q=50)	0.1251	Weak
Gaussian noise ($\sigma=10$)	0.1786	Weak
Gaussian noise ($\sigma=25$)	0.1090	Weak
Rotation (5°)	0.0006	Weak
Brightness (+50)	0.0482	Weak

The highest NCC after attack was 0.3690, recorded under JPEG compression at quality factor 75. NCC values for the remaining five conditions were: 0.1251 (JPEG quality factor 50), 0.1786 (Gaussian noise $\sigma=10$), 0.1090 (Gaussian noise $\sigma=25$), 0.0006 (rotation 5°), and 0.0482 (brightness +50). All six values fall below the 0.50 threshold used to classify watermark recovery as Moderate or higher.

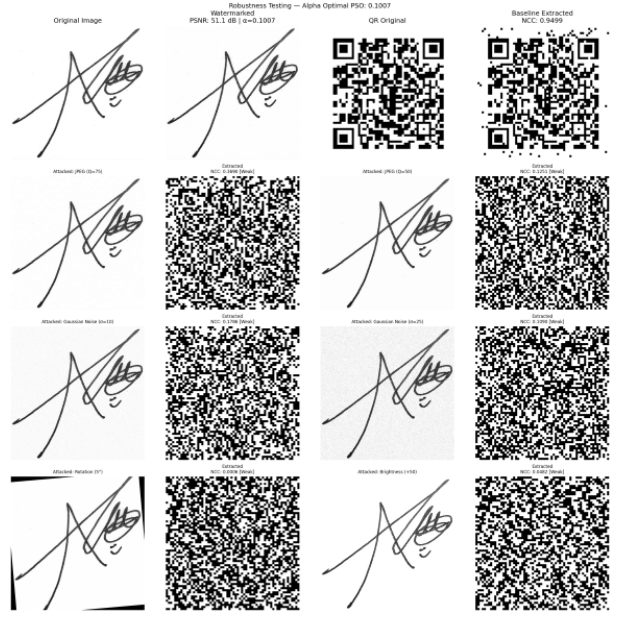


Figure 4. Visualization Robustness Testing

IV. DISCUSSION

The 11.90 dB increase in PSNR between the manually configured baseline (39.25 dB) and the PSO-optimized configuration (51.15 dB) indicates that the search procedure identified an α value associated with lower distortion than the manually selected 0.05. This result is consistent with prior reports that PSO-based parameter search produces PSNR values different from manually configured baselines in DFT-based watermarking [5].

The relationship between PSNR and NCC observed in this study did not follow a proportional pattern. While PSNR increased by 11.90 dB after optimization, the highest post-attack NCC value (0.3690, under JPEG quality factor 75) remained below the 0.50 threshold used to classify recovery as Moderate. Four of the six tested conditions yielded NCC values below 0.20, and rotation by 5° yielded an NCC of 0.0006. This pattern indicates that an increase in PSNR was not accompanied by a corresponding increase in NCC under the tested attack conditions.

A contributing factor is the extraction procedure used in this study, defined in (9), which computes the watermark by subtracting the cover image's DFT coefficients from those of the attacked watermarked image. Under JPEG compression, Gaussian noise, rotation, or brightness adjustment, the DFT coefficients of the attacked image differ from those of the unattacked watermarked image in ways not limited to the embedded region. Because (9) assumes that the only difference between $F_w'(u,v)$ and $F_{\text{shift}}(u,v)$ is the embedded term $\alpha \cdot Q(u,v)$, any additional coefficient change introduced by the attack is included in the computed difference, which is then divided by α and treated as part of the

recovered watermark. This describes a property of the non-blind subtraction-based extraction method used in this study, rather than a property specific to the cover image or the QR Code payload.

This finding differs from the robustness levels reported in [5], where PSO-optimized DFT watermarking was evaluated under JPEG compression and noise without reporting NCC values below 0.50 across the tested conditions. One difference between the present study and [5] is the extraction method: the present study used coefficient subtraction requiring the original cover image, while robustness comparisons in frequency-domain watermarking literature more commonly report results for blind extraction methods that do not require the original image during extraction [3]. The fitness function in (6) was designed to weight NCC at 0.75 relative to PSNR at 0.25 during optimization; despite this weighting, the optimizer converged to an α value (0.1007) that did not produce NCC values above 0.50 under five of six tested attack conditions. This indicates that, within the search space and attack conditions used during optimization, no tested value of α produced both PSNR above 30 dB and NCC above 0.50 across the four attack types used in the fitness calculation.

The QR Code payload used in this study encodes identity information at a fixed 64×64 pixel resolution. Sanivarapu et al. embedded a QR Code containing a cryptographic key pair using a method not restricted to the DFT domain [9], and reported extraction results without applying the JPEG compression, Gaussian noise, and rotation conditions used in the present study. A direct numerical comparison between the two studies is not possible due to differences in embedding domain, payload size, and tested attack conditions.

These results indicate that, under the tested configuration, mid-frequency DFT embedding combined with PSO optimized α produced measurable improvement in PSNR but did not produce NCC values above 0.50 under five of six tested attack conditions. The non-blind subtraction based extraction method is identified as a contributing factor to this outcome.

V. CONCLUSION

This study analyzed the imperceptibility and robustness characteristics of a QR Code watermarking scheme applied to digital signature images, using mid-frequency DFT embedding with PSO-based parameter optimization. The analysis produced two principal findings.

First, PSO optimization of the embedding strength parameter α yielded a PSNR of 51.15 dB and an NCC of 0.9499 under no-attack conditions, representing an 11.90 dB improvement in imperceptibility relative to the

manually configured baseline ($\alpha = 0.05$, PSNR = 39.25 dB). This result indicates that automated parameter search via PSO identifies embedding configurations that produce lower distortion than manually selected values, without requiring exhaustive trial-and-error.

Second, under six simulated attack conditions, JPEG compression at quality factors 75 and 50, Gaussian noise at standard deviations 10 and 25, rotation at 5°, and brightness adjustment of +50 NCC values ranged from 0.0006 to 0.3690, all below the 0.50 threshold used to classify watermark recovery as Moderate or higher. The non-blind, subtraction-based extraction method employed in this study is identified as a contributing factor, as coefficient changes introduced by an attack are not separable from the embedded watermark term during extraction. This finding is consistent with the broader observation in frequency-domain watermarking literature that non-blind extraction methods are inherently sensitive to signal modifications that alter DFT coefficients beyond the embedded region.

These results indicate that mid-frequency DFT embedding with PSO-optimized α produces measurable and consistent improvement in imperceptibility, while robustness under attack conditions remains constrained by the extraction method rather than the embedding strategy alone. Future work may evaluate blind extraction methods that do not require the original cover image, may test hybrid transform domain approaches such as DFT combined with Discrete Wavelet Transform (DWT) or Singular Value Decomposition (SVD), and may extend this analysis to other document image types to further investigate the relationship between cover image texture complexity and watermark robustness.

DECLARATIONS

Conflict of Interest

The authors declare no conflict of interest.

CRediT Authorship Contribution

Azwa Fazilatunnisa: Conceptualization, Methodology, Software, Writing original draft, Visualization, Investigation, Formal analysis; Didi Rosiyadi: Supervision, Validation, Writing, Review and Editing, Resources; M. Iman Wahyudi: Supervision, Validation, Writing, Review and Editing.

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